

NISTPQC is so much fun! 10900qmmP

Lorenz Panny

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Costa Adeje, Tenerife, 31 January 2018

- ▶ Not a competition.
- ▶ 69 submissions published on December 21st 2017.
- ▶ First complete break: 3 hours later.

BIG QUAKE. BIKE. CFPKM. Classic McEliece. Compact LWE. CRYSTALS-DILITHIUM. CRYSTALS-KYBER. DAGS. Ding Key Exchange. DME. DRS. DualModeMS. Edon-K. EMBLEM & R.EMBLEM. FALCON. FrodoKEM. GeMSS. Giophantus. Gravity-SPHINCS. Guess Again. Gui. HILA5. HiMQ-3. HK17. HQC. KINDI. LAC. LAKE. LEDAkem. LEDApkc. Lepton. LIMA. Lizard. LOCKER. LOTUS. LUOV. McNie. Mersenne-756839. MQDSS. NewHope. NTRUEncrypt. pqNTRUSign. NTRU-HRSS-KEM. NTRU Prime. NTS-KEM. Odd Manhattan. OKCN/AKCN/CNKE. Ouroboros-R. Picnic. pqRSA encryption. pqRSA signature. pqsigRM. QC-MDPC KEM. qTESLA. RaCoSS. Rainbow. Ramstake. RankSign. RLCE-KEM. Round2. RQC. RVB. SABER. SIKE. SPHINCS+. SRTPI. Three Bears. Titanium. WalnutDSA.

(slide stolen from Daniel J. Bernstein)

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Gravity-SPHINCS. **Guess Again**. Gui. **HILA5**. HiMQ-3. **HK17**.
HQC. KINDI. LAC. LAKE. LEDAkem. LEDApkc. Lepton. LIMA.
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UNCONDITIONALLY SECURE PUBLIC-KEY ENCRYPTION

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(WITH POSSIBLE DECRYPTION ERRORS)

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Guess Again

[...] legitimate sender has an advantage over the eavesdropper since the sender [...] knows exactly what the transmitted secret bit is. [...] instead of making the receiver guess the transmitted bit we make the sender guess the receiver's decryption key [...].

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Alice **transmits** a single bit $m \in \{0, 1\}$ to Bob:

- ▶ Select $\leq \xleftarrow{\text{random}} \{<, >\}$ and $s \xleftarrow{\text{random}} \{f, g\}$.
- ▶ Pick $a \xleftarrow{\text{random}} \{B \dots n - 1\}$ and let $A := \text{random_walk}(a, s)$. Repeat this until $A \leq B$.
- ▶ If $s = f$, send (m, a) . Else send $(1 \oplus m, a)$.

Repeat many times to increase success probability.

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Argument: Bit m is flipped with **probability** $\frac{1}{2}$, thus secure. (?)

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Distribution of a conditional on $(\leq, s):$

s	A	a	flip?
f	$< B$	slightly biased towards B	0
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\implies In expectation, a of 'flipped' ciphertexts are smaller.

Guessed Again ✓

```
def recover_bit(ct, bit):
    assert bit < len(ct) // 4000
    ts = [struct.unpack('BB', ct[i:i+2])]
        for i in range(4000*bit, 4000*(bit+1), 2)]
    xs, ys = [a for a, b in ts if b == 1], [a for a, b in ts if b == 2]
    return sum(xs) / len(xs) >= sum(ys) / len(ys)

def decrypt(ct):
    res = sum(recover_bit(ct, b) << b
        for b in range(len(ct) // 4000))
    return int.to_bytes(res, len(ct) // 4000 // 8, 'little')
```

Guessed Again ✓

*[...] our protocol is IND-CCA2 secure against any **passive** adversary, even computationally unbounded one.*

*[...] “Computationally unbounded” here includes all possible computers, **quantum or not**.*

— ‘Guess Again’ NISTPQC submission document

- ▶ Chebyshev polynomials:

$$T_0 = 1$$

$$T_1 = t$$

$$T_n = 2t \cdot T_{n-1} - T_{n-2}$$

- ▶ Commutative semigroup under composition:

$$T_a \circ T_b = T_b \circ T_a = T_{a \cdot b}$$

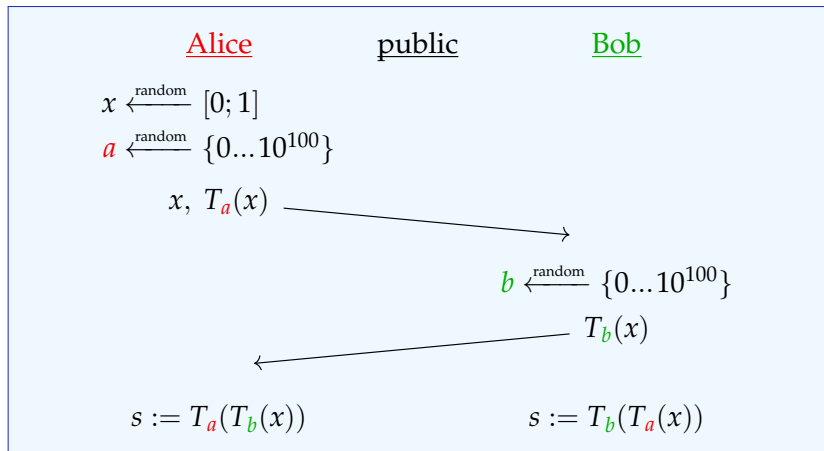
...screams Diffie-Hellman, but it is **secure**?

Fear not: for behold, I bring you good tidings of great joy!

*Given x , $y = T_a(x)$, there is **no efficient way** to compute the secret parameter a from $T_a(x)$, even if a quantum computer [...] is used for the attack, as will be shown.*

— 'RVB' NISTPQC submission document

RVB



All computations using high-precision floating point numbers.

► Trigonometry:¹

$$\cos(n \cdot \alpha) = T_n(\cos \alpha) \quad \forall \alpha \in \mathbb{R}.$$

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- ▶ **Therefore** [Bergamo–D’Arco–De Santis–Kocarev 2004, arXiv:cs/0411030]

$$\begin{aligned} T_n(x) &= y \\ \iff \cos(n \cdot \arccos x) &= y \end{aligned}$$

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- ▶ B-D'A-DS-K now implicitly assume α and β are **rational** and multiply by $d = \text{lcm}(\text{denominators})$:

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- ▶ Extremely **unrealistic**: $\arccos(\mathbb{Q}) \cap \mathbb{Q} = \{0\}$.
 \implies **Rounding errors** all over the place.

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*The methods to uncover the secret do definitely not work. A **solvable diophantine equation** derived from the inverse cosine function **does not exist**.*

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[...]

Several hundred years ago everybody strongly believed that the sun rotates around the earth.

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Let $\alpha, \beta \in \mathbb{R}$ and $k \in \mathbb{Z}$ such that $\alpha + k\beta \in \mathbb{Z}$.

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Let K be an upper bound for $|k|$ and $B \approx K^2$.

The **lattice** spanned by the rows of

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with $|\varepsilon| \ll B$. This corresponds to the relation

$$[aB] + k'[bB] \equiv \varepsilon \pmod{B},$$

and division by B yields

$$a + k'b \approx 0 \pmod{\mathbb{Z}}.$$

```
def recover(pk):
    Tx, x = map(RealField(10**4), pk.split('\0')[2:])

    a = arccos(Tx) / arccos(x)
    b = 2*pi / arccos(x)

    # find an integer k such that a + k * b is close to an integer
    B = 10**(len(pk)//2)
    M = matrix([[B, 0, round(a*B)], [0, 1, round(b*B)], [0, 0, B]])
    for l in M.LLL().rows():
        if l[0]:
            k = sign(l[0]) * l[1]
            break

    guess = abs(round(a + k * b))

    # brute-force a small range in case we are slightly off
    for d in range(256):
        for s in (-1, +1):
            if abs(cos((guess + s * d) * arccos(x)) - Tx) < 1e-10:
                return guess + s * d
```

*[...] using the Lenstra–Lenstra–Lovász (LLL) lattice basis reduction algorithm is something that we didn't have on our radar screen. It **successfully breaks** the entire encryption scheme in **almost no time**.*

The attack is reproducible and well-documented. Congratulations for this great work!

— 'RVB' authors' withdrawal notice

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RaCoSS

- ▶ $n = 2400, k = 2060$.
- ▶ Public parameter: fixed random matrix $H \in \mathbb{F}_2^{(n-k) \times n}$.
- ▶ **Secret key** is sparse $S \in \mathbb{F}_2^{n \times n}$. **Public key** is $T = H \cdot S$.

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- ▶ Hash function wrhf maps to n -bit strings of weight 3.
- ▶ **Signing** a message m : Pick a low-weight $y \in \mathbb{F}_2^n$.
Compute $v = Hy$, $c = h(v, m)$, $z = Sc + y$. Output (z, c) .

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Compute $v = Hy$, $c = h(v, m)$, $z = Sc + y$. Output (z, c) .
- ▶ **Verifying** $m, (z, c)$: Check that $\text{weight}(z) \leq 1564$.
Compute $v' = Hz + Tc$. Check that $h(v', m) = c$.

Implementation bug:

```
unsigned char  c[RACOSS_N];
unsigned char  c2[RACOSS_N];

/* ... */

for( i=0 ; i<(RACOSS_N/8) ; i++ )
    if( c2[i] != c[i] )
        /* fail */

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...compares only the first 300 coefficients!

Thus, a signature with $c[0\dots299] = 0$ is accepted for

$$\binom{2100}{3} / \binom{2400}{3} \approx 67\%$$

of all messages.

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- ▶ another message signed by the **first KAT**:

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- ▶ Pick $n - k$ columns of H that form an invertible matrix H_1 .²
This can be written as $H_1 = HC$ with $C \in \mathbb{F}_2^{n \times (n-k)}$.³

²Approximately 29% of all $(n - k) \times (n - k)$ matrices over \mathbb{F}_2 are invertible.

³For the proposed H , the first $n - k$ columns of H work: $C = (I_{n-k} \mid 0)^T$.

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- ▶ Compute $z_1 := H_1^{-1}(v + Tc)$ and $z := Cz_1$.
- ▶ Then $Hz = HCz_1 = H_1z_1 = v + Tc$ as desired.
- ▶ Expected **weight** of z is $\approx \frac{n-k}{2} = 170 \ll 1564$.
- ▶ Properly generated signatures have $\text{weight}(z) \approx 261$.

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Cautionary notice



These stunts were performed by [trained professionals](#).

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You should totally try this at home!

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Thanks!